

PHYSICS
PAPER - II

Time Allowed : 3 hours

Full Marks : 100

Marks for each question is indicated against it.

Attempt any 5 (five) questions taking not more than 3 (three) questions from each Part.

PART - A

1. (a) The one-dimensional wave equation for a free particle of mass m is given by

$$\frac{-\hbar^2 \partial^2 \psi(x,t)}{2m \partial x^2} = i\hbar \frac{\partial \psi(x,t)}{\partial t}$$

where $\psi(x,t)$ represents the wave function of the particle. Solve the equation by the method of separation of variables. (7)

- (b) The wave function for a particle confined in a one-dimensional box of length L is given

by $\psi(x) = A \sin \frac{n\pi x}{L}$. Normalize the wave function and evaluate the expectation values of its momentum. (5)

- (c) (i) Find the probability that a particle trapped in a box L wide can be found between $0.45L$ and $0.55L$ for the first excited state.

(ii) Find the expectation value $\langle x \rangle$ of the position of a particle trapped in a box L wide. (4+4=8)

2. (a) Write down the Schrödinger equation of a one-dimensional harmonic oscillator, solve the equation to obtain the energy eigen values. Also draw a diagram to represent the energy levels and wave functions of the lowest four states of the linear harmonic oscillator. (8+4=12)

- (b) If L_x, L_y, L_z are the Cartesian components of an angular momentum operator and L is their resultant, evaluate the following commutators $[L_x, L_y], [L_y, L_z], [L_z, L_x]$ and $[L^2, L_x]$. (8)

3. (a) Describe the Stern-Gerlach experiment. Give the explanation to the results of this experiment based on quantum mechanical theory. (10)

- (b) Discuss the general quantum mechanical theory of the Anomalous Zeeman effect, with special reference to the sodium D lines. (10)

4. (a) What is Raman Effect? Explain how it is used in the study of molecular structure and tri-atomic molecules. (10)
- (b) Obtain an expression for the resonance condition in NMR. (10)

PART - B

5. (a) What do you understand by the term Binding energy of a nucleus? Show the variation of Binding energy per nucleon with mass number of a nucleus and discuss its characteristics. Calculate the binding energy of a Helium nucleus.
Given mass of a helium atom = 4.002603 amu, mass of a hydrogen atom = 1.007825 amu and the mass of a neutron = 1.08665 amu. (2+4+1=7)
- (b) Discuss how the Shell model of a nucleus could explain the origin of Magic numbers in a nucleus. (7)
- (c) Discuss the basic theory, construction and working of a nuclear reactor. (6)
6. (a) What is a neutrino? How does it differ from its anti-particle? Explain how the neutrino hypothesis solves the apparent breakdown of conservation of momentum and energy in β -decay. (1+1+3=5)
- (b) What is the difference between fermions and bosons? Which of the following particles are fermions and which are bosons? (1+4=5)
 μ^+ , Λ^0 , K^0 , Σ^+
- (c) Check if the following reactions are allowed or forbidden: (4)
- (i) $\pi^- + p = \Lambda^0 + \pi^0$
- (ii) $p + \bar{p} = 2\pi^+ + 2\pi^- + 2\pi^0$
- (d) What are coloured quarks and gluons? State the properties of three generations of quarks and leptons. (2+2+2=6)
7. (a) Distinguish between metals, insulators and semi-conductors on the basis of band theory of solids. Why does a semi-conductor act as an insulator at 0K? (10)
- (b) What are Type I and Type II superconductors? Describe the effect of an external magnetic field on the superconducting state of a material. (10)
8. (a) Draw the static characteristics of a field effect transistor (FET) and explain the different regions. (7)
- (b) What is an OP-AMP? Describe the workings of the inverting and non-inverting operational amplifiers. (7)
- (c) Give the truth tables of two-input OR and AND logic gates. Draw electrical circuits representing each one of them. (6)